

- Discuss finding an inverse via Gauss-Jordan Elimination.
- Discuss rotation matrices.

$$R_\theta = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

Note that

$$\det(R_\theta) = \cos^2 \theta + \sin^2 \theta = 1$$

so

$$R_\theta^{-1} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

Check It!

**Proposition 1.** *Suppose that  $A$  and  $AB$  are invertible. Then  $B$  is also invertible.*

*Proof.* Since  $A$  is invertible, there exists  $A^{-1}$  such that  $A^{-1}A = AA^{-1} = I$ . Similarly,  $AB$  is invertible so there exists some  $C$  such that  $C(AB) = (AB)C = I$ . By using the associativity of matrix multiplication, we get  $C(AB) = (CA)B = I$ , and therefore  $B$  has an inverse.  $\square$